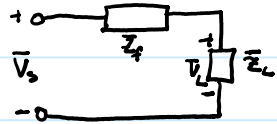


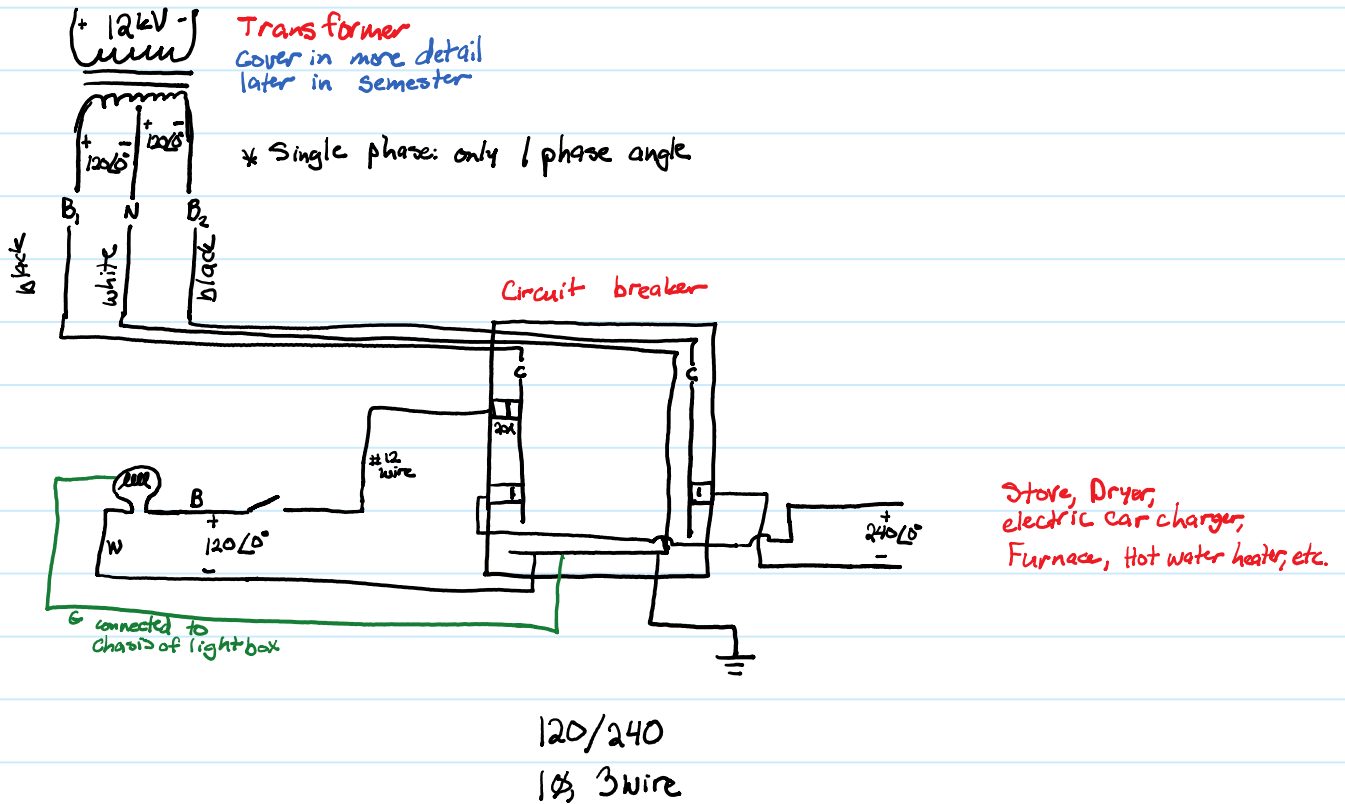
Note: Feeder system: wires have impedances



Last time:

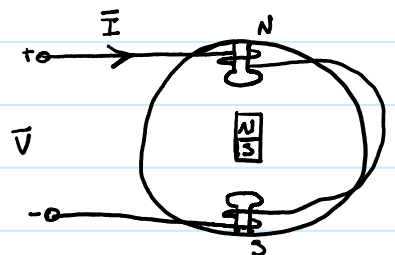
- 1) Power triangle
- 2) Computing power
- 3) Conservation of complex power and power factor correction

- Today:
- 1) Residential single phase (1ϕ) power
 - 2) Approximating 2ϕ power
 - 3) Intro to 3ϕ power



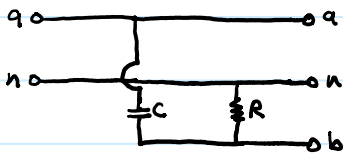
* 1ϕ has problems with motors:

- a) pulsating power
 - b) no starting torque
- Repulsive and attractive forces act through center giving no torque.
 - However, if something started rotation, it would continue.



* This problem can be fixed by adding a second phase. How?

Circuit to motor:



$$\bar{I}_b = \frac{\bar{V}_{an}}{R - j\frac{1}{\omega C}}$$

$$\begin{aligned} \bar{V}_b = R\bar{I}_b &\Rightarrow \bar{V}_b = \left(\frac{R}{R - j\frac{1}{\omega C}} \right) \bar{V}_{an} \\ &= \left(\frac{R^2 + jR(\frac{1}{\omega C})}{R^2 + (\frac{1}{\omega C})^2} \right) \bar{V}_{an} \\ &= \left(\frac{R^2}{R^2 + (\frac{1}{\omega C})^2} + j \frac{R(\frac{1}{\omega C})}{R^2 + (\frac{1}{\omega C})^2} \right) \bar{V}_{an} \end{aligned}$$

for $(\frac{1}{\omega C}) \gg R$ or $\frac{1}{R} \gg \omega C$

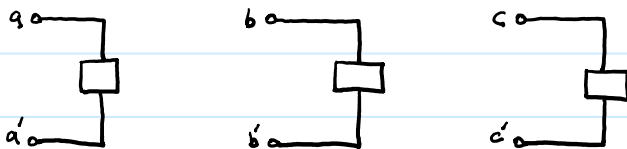
$$\bar{V}_{bn} \approx \left(\frac{jR(\frac{1}{\omega C})}{R^2 + (\frac{1}{\omega C})^2} \right) \bar{V}_{an}$$

* Phase is shifted by 90°. This is (approximate) 2φ power

True 2φ: $\bar{V}_{an} = V\angle 0^\circ$
 $\bar{V}_{bn} = V\angle 90^\circ$ } Results in rotating magnetic field
 * More details later in semester

* 2x power as 1φ
 * 2x wires as 1φ
 (4 vs. 2)

Even better: 3φ



Positive Sequence
 a-b-c

$$V_{a'a} = V_m \cos(\omega t)$$

$$V_{b'b} = V_m \cos(\omega t - 120^\circ)$$

$$V_{c'c} = V_m \cos(\omega t + 120^\circ)$$

Negative Sequence

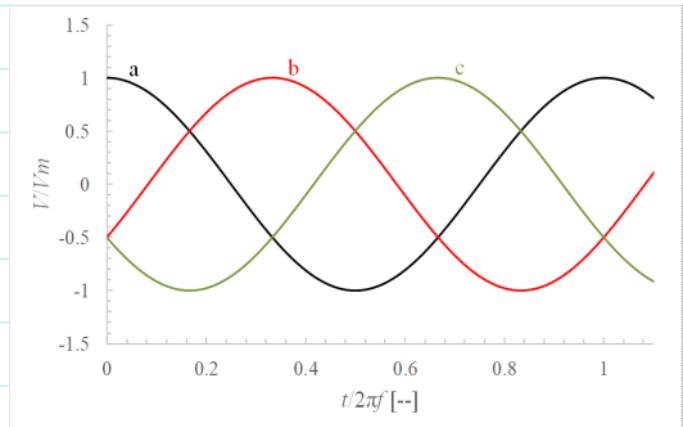
a-c-b

$$V_{a'a} = V_m \cos(\omega t)$$

$$V_{b'b} = V_m \cos(\omega t + 120^\circ)$$

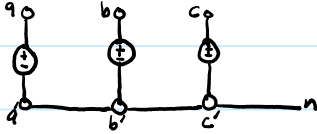
$$V_{c'c} = V_m \cos(\omega t - 120^\circ)$$

a-b-c sequence

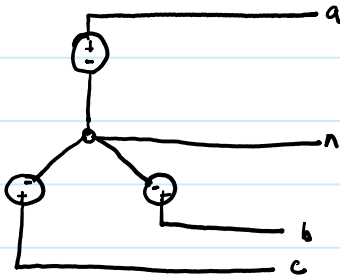


Connecting the 3 phases

1) Wye

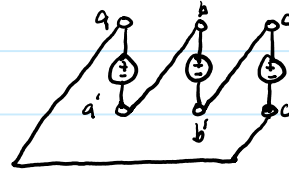


Conventional diagram

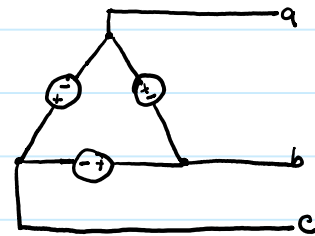


$$i_n = i_a + i_b + i_c$$

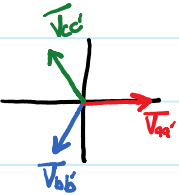
2) Delta



Conventional diagram



$$V_{ac'} = V_{aa'} + V_{bb'} + V_{cc'} = 0$$

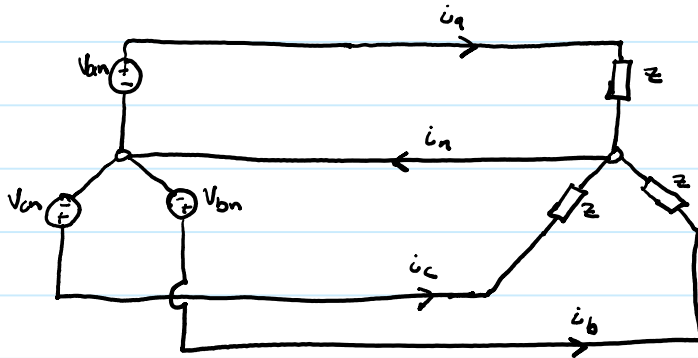


* Loads can also be connected in wye or delta

		Source	
		Wye	Delta
Load	Wye	Wye-Wye	Delta-Wye
	Delta	Wye-Delta	Delta-Delta

Wye-Wye and Wye-Delta are most common connections.

Wye Source to Wye Load



* Balanced load:
all impedances equal